

Machine Learning

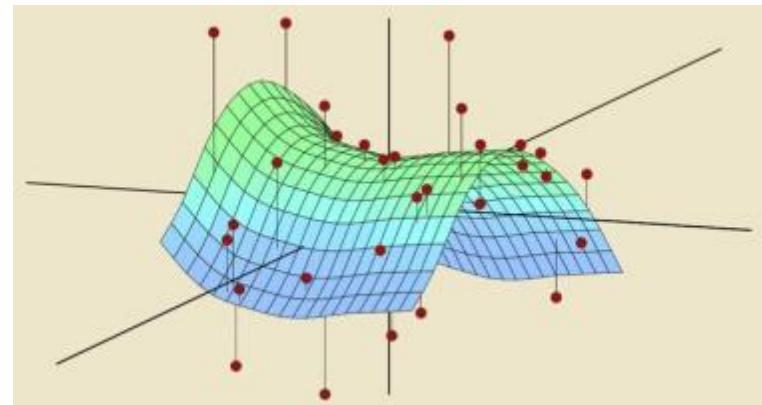
Course Introduction

- Three years old course edition ...
 - Same name & program (PAMI)
 - New book (somehow easier)
 - New approach (more practical)
- It worked out !!!
- This year we have a new course edition ...
 - I does not change much
- Lectures given by:
 - Matteo Matteucci (Lecturer): matteo.matteucci@polimi.it
 - Davide Eynard (Teaching Assistant): davide.eynard@polimi.it



- Topics covered during the course

- Statistical Learning Theory
- Regression methods
- Classification methods
- Clustering methods



- Course organization

- For each topic, on average: 6hL + 4hE + 2hLab
- Lab in class with R, you can use your laptop



- Detailed schedule (Tentative) available online already!

http://chrome.ws.dei.polimi.it/index.php/Machine_Learning

- Book for this year edition

- Same authors of ESL (the best!)
- Easier than ESL
- Practical perspective
- Labs and Exercises using the R language
- Available online as pdf

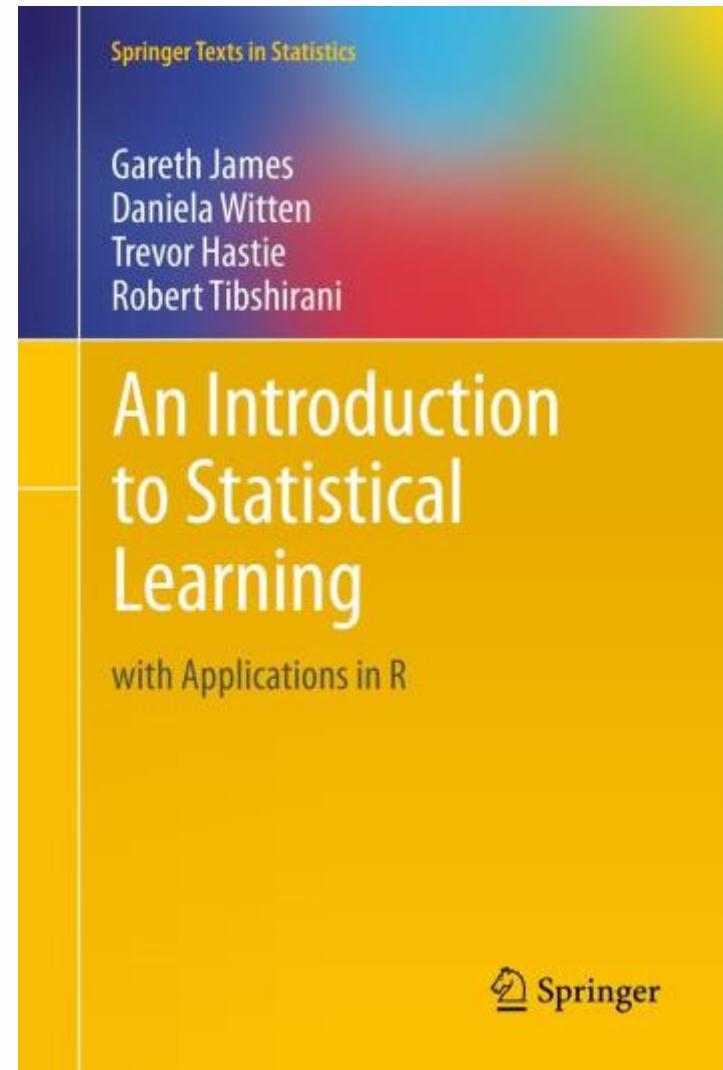
www.statlearning.com

- Slides from the teachers

- Taken from the book
- Updated after the lectures

- Contributed material (TBD)

- Notes, exercises and questions from students? [google docs]



- The exam grade is composed by a written exam & homework
 - WE - Written Exam is compulsory
 - 2 Theoretical questions + 2 Practical Exercises (no R code)
 - Covering the 4 topics previously introduced
 - HW - Homeworks are NOT compulsory, but ...
 - ... they help you in understanding the course and prepare WE
 - ... they get you in the “nitty gritty” of implementations
 - ... they can only increase the final grade!
 - Final GRADE combines the two
 - GRADE = $\text{MAX}(\text{WE}, 0.7*\text{WE} + 0.3\text{HW})$

- ...

- 1. Many statistical learning methods are relevant and useful in a wide range of academic and non-academic disciplines, beyond just the statistical sciences.*

 - Rather than attempting to consider every possible approach (an impossible task), we concentrate on presenting the methods that we believe are most widely applicable.
- 2. Statistical learning should not be viewed as a series of black boxes.*

 - No single approach will perform well in all possible applications. We attempt to carefully describe the model, intuition, assumptions, and trade-offs behind each of the methods that we consider.

3. *While it is important to know what job is performed by each cog, it is not necessary to have the skills to construct the machine in the box!*
 - We minimize discussion of technical details related to fitting procedures and theoretical properties. We assume the reader is comfortable with basic mathematical concepts, but we do not assume a graduate degree in mathematical science.
4. *We presume that the reader is interested in applying statistical learning methods to real-world problems.*
 - We devote some time to R computer labs. In each lab, we walk through a realistic application of the methods considered during the lectures.

Three Reference Scenarios (Wage)

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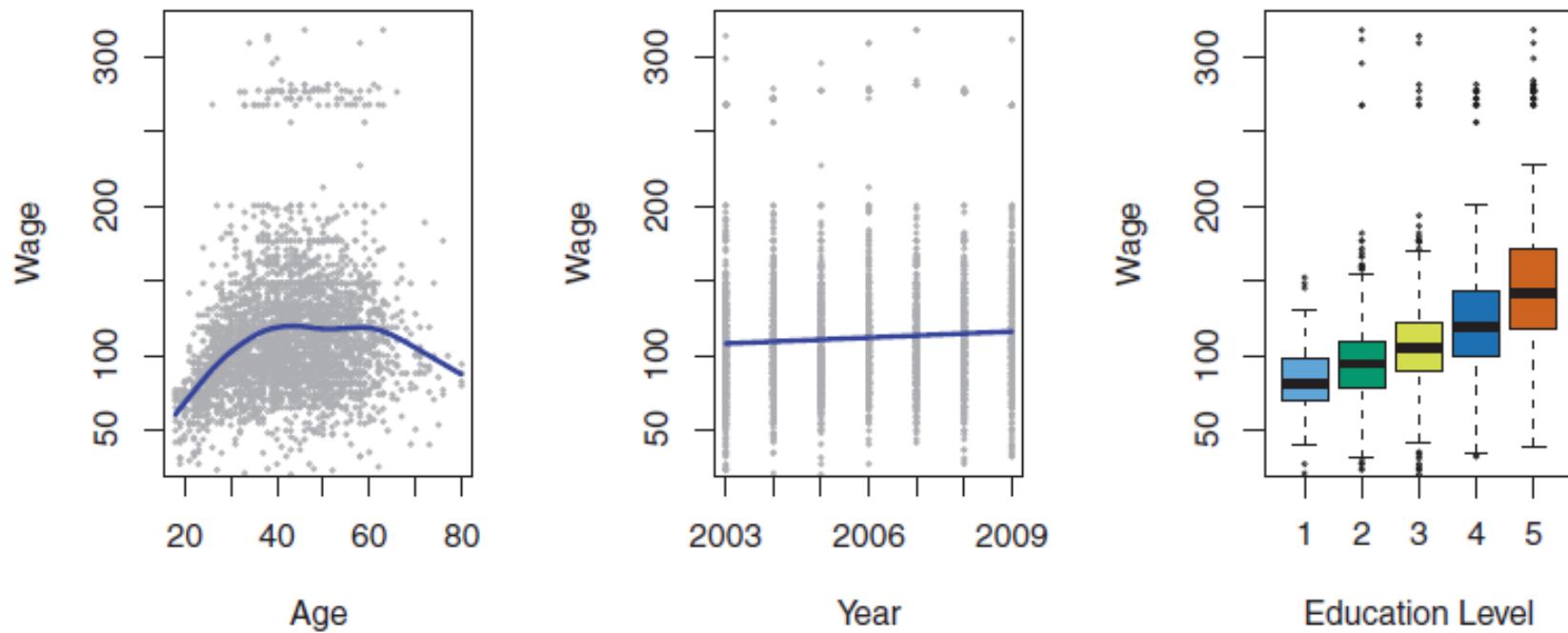
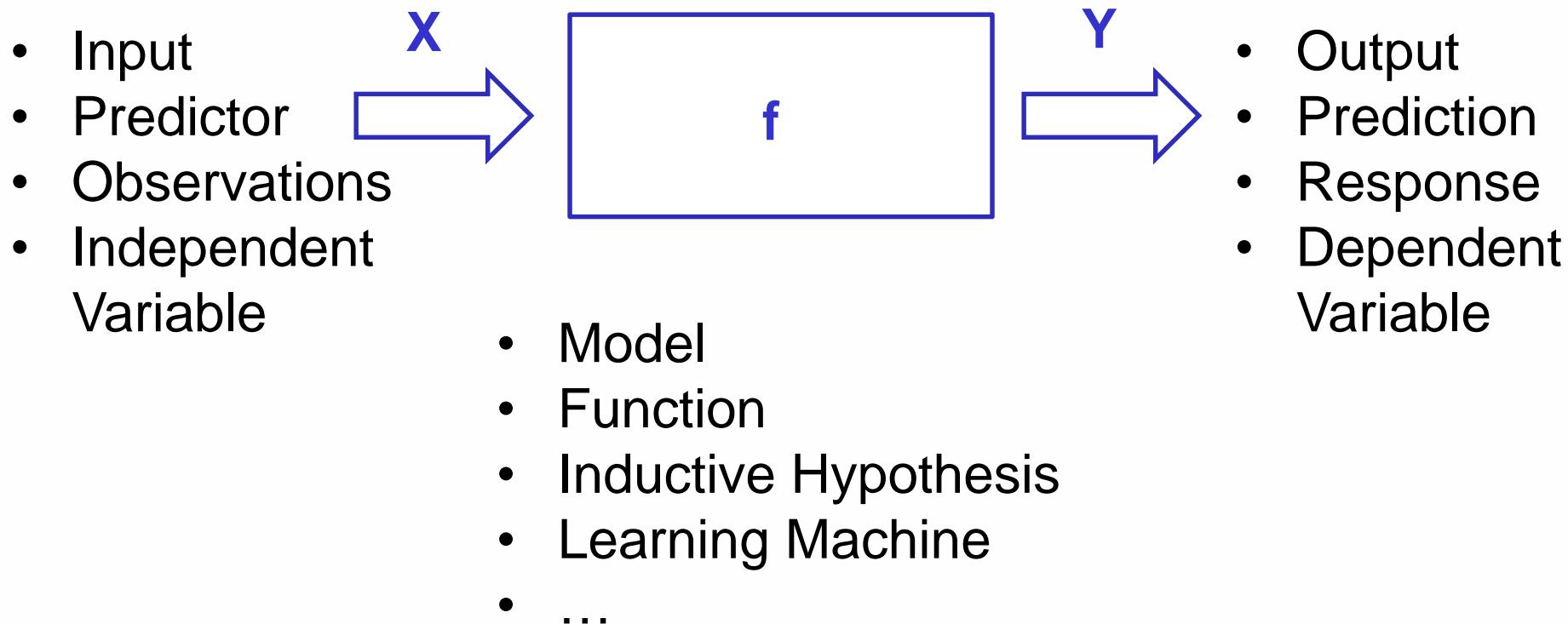


FIGURE 1.1. Wage data, which contains income survey information for males from the central Atlantic region of the United States. Left: wage as a function of age. On average, wage increases with age until about 60 years of age, at which point it begins to decline. Center: wage as a function of year. There is a slow but steady increase of approximately \$10,000 in the average wage between 2003 and 2009. Right: Boxplots displaying wage as a function of education, with 1 indicating the lowest level (no high school diploma) and 5 the highest level (an advanced graduate degree). On average, wage increases with the level of education.



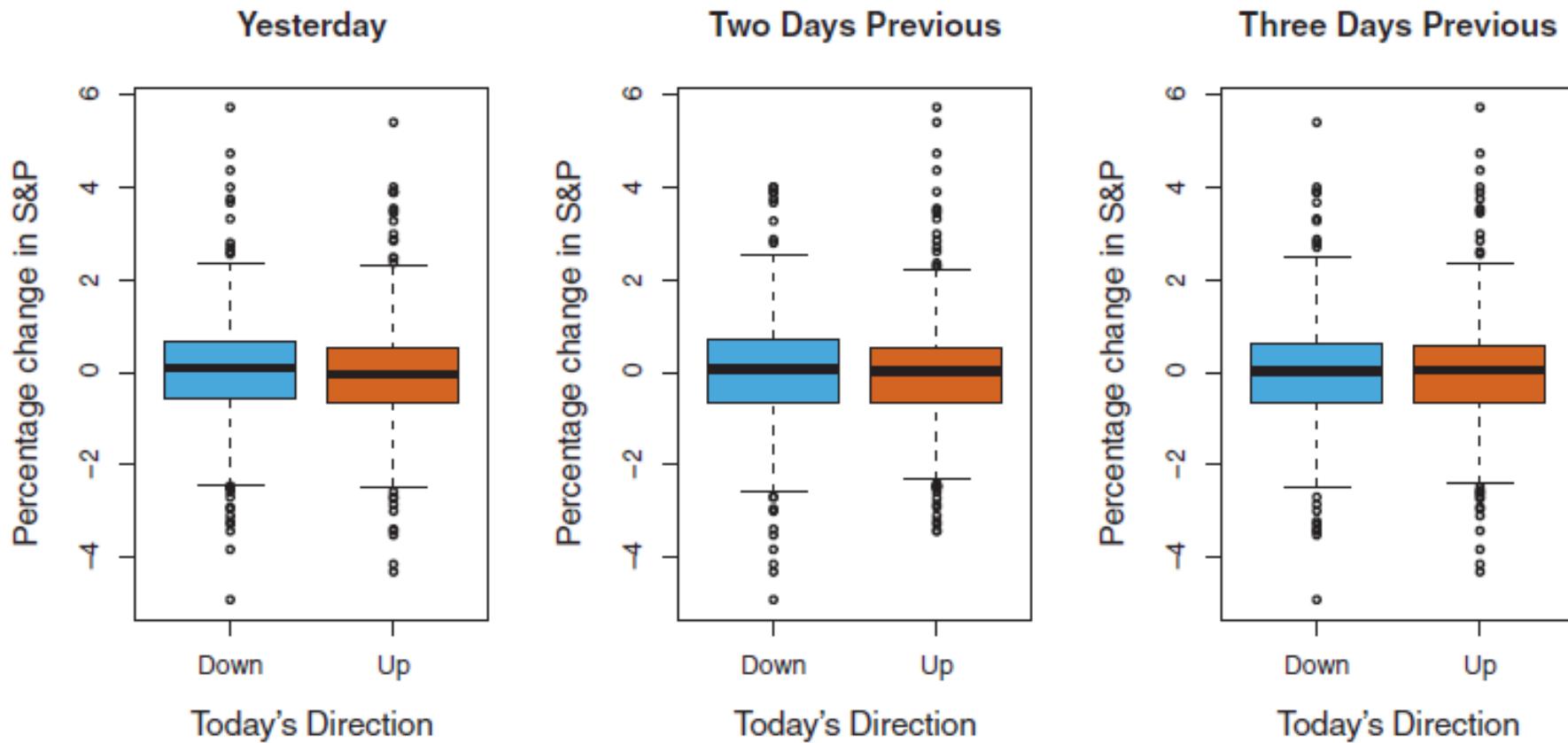


FIGURE 1.2. Left: Boxplots of the previous day's percentage change in the S&P index for the days for which the market increased or decreased, obtained from the Smarket data. Center and Right: Same as left panel, but the percentage changes for 2 and 3 days previous are shown.

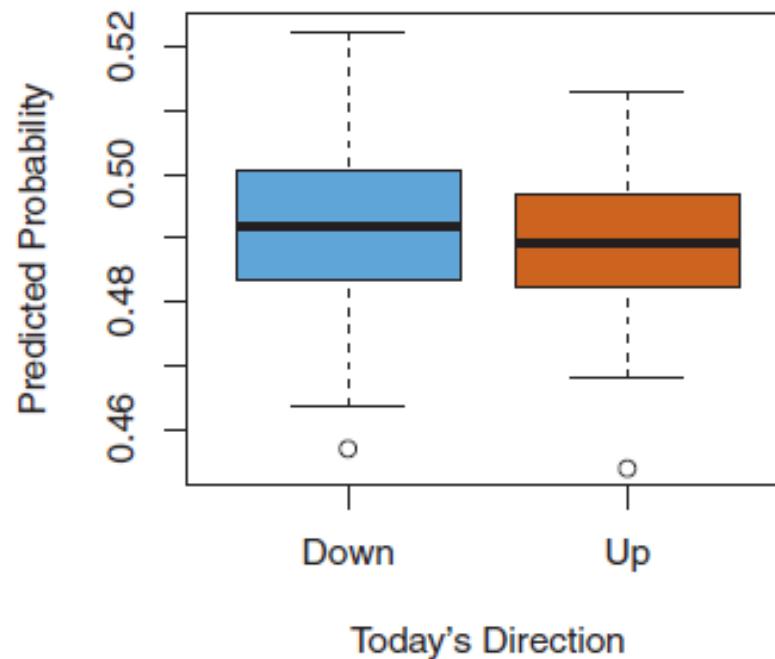
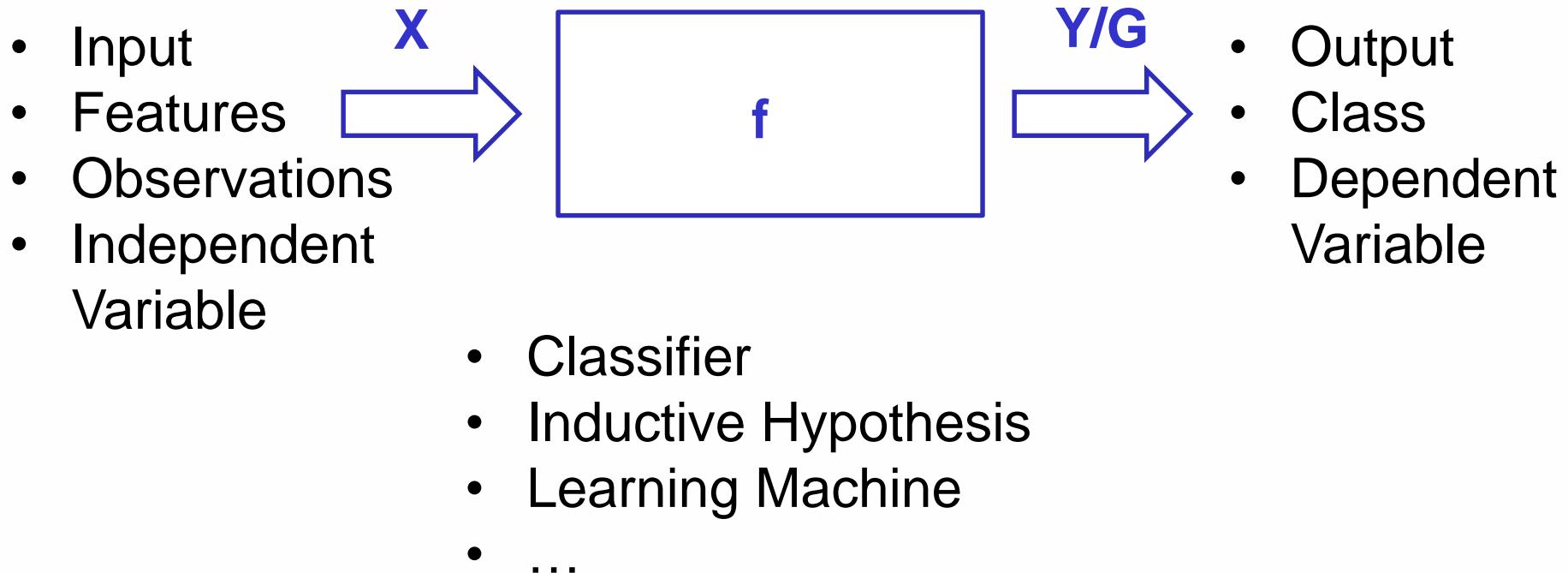


FIGURE 1.3. We fit a quadratic discriminant analysis model to the subset of the Smarket data corresponding to the 2001–2004 time period, and predicted the probability of a stock market decrease using the 2005 data. On average, the predicted probability of decrease is higher for the days in which the market does decrease. Based on these results, we are able to correctly predict the direction of movement in the market 60% of the time.



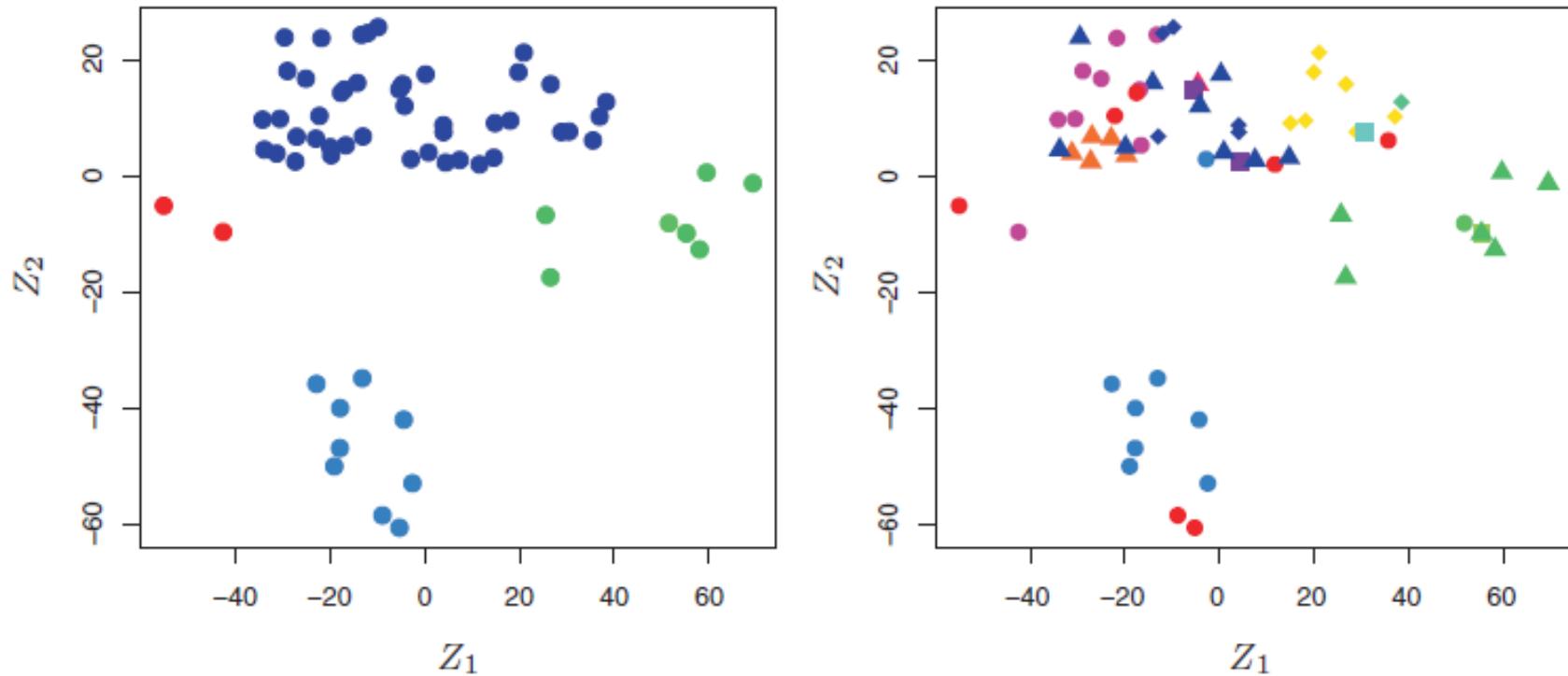
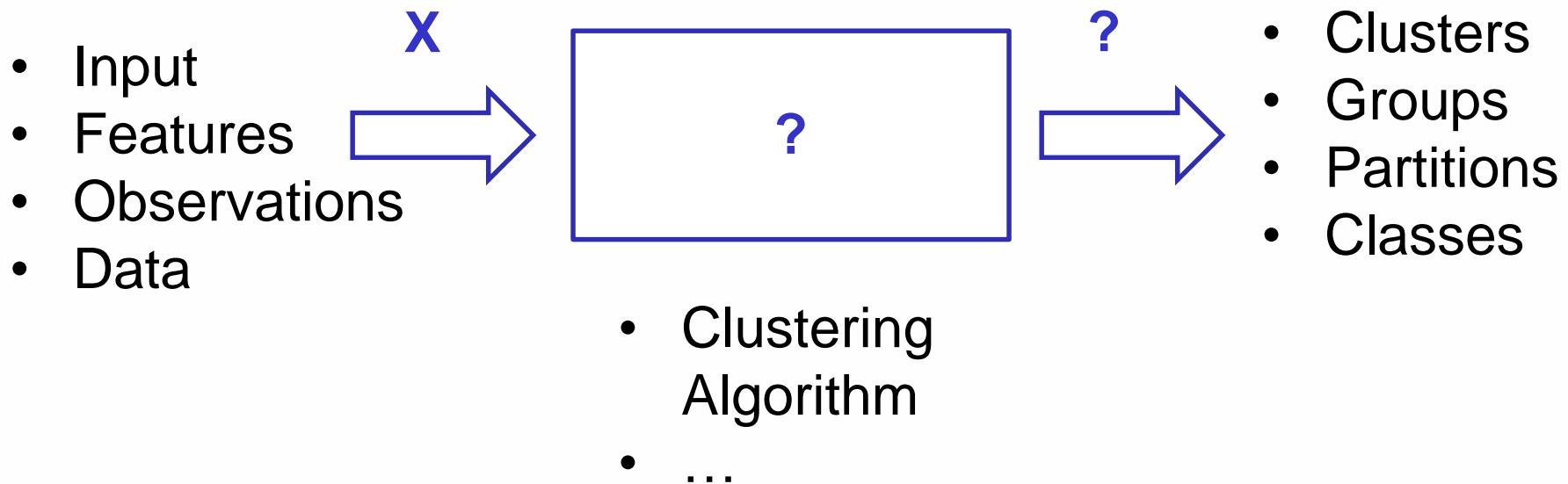
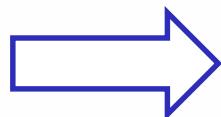


FIGURE 1.4. Left: Representation of the NCI60 gene expression data set in a two-dimensional space, Z_1 and Z_2 . Each point corresponds to one of the 64 cell lines. There appear to be four groups of cell lines, which we have represented using different colors. Right: Same as left panel except that we have represented each of the 14 different types of cancer using a different colored symbol. Cell lines corresponding to the same cancer type tend to be nearby in the two-dimensional space.

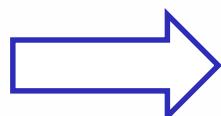


$$X \in \mathbb{R}^p$$


Regression

$$Y \in \mathbb{R}$$


Continuous
Output

$$X \in \mathbb{R}^p$$


Classification

$$Y \in \{\Omega_0, \Omega_1, \dots, \Omega_K\}$$


Discrete
Output

$$X \in \mathbb{R}^p$$


Clustering

$$Y \in \wp(X)$$


Partitions

- Input and Output Matrixes

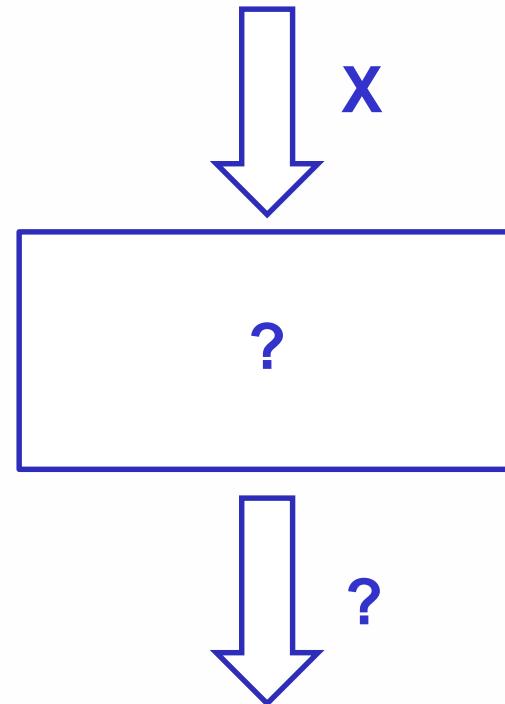
$$\mathbf{X} = \begin{pmatrix} x_{11} & x_{12} & \dots & x_{1p} \\ x_{21} & x_{22} & \dots & x_{2p} \\ \vdots & \vdots & \ddots & \vdots \\ x_{n1} & x_{n2} & \dots & x_{np} \end{pmatrix} \quad \mathbf{y} = \begin{pmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{pmatrix}$$

- Data sample

$$x_i = \begin{pmatrix} x_{i1} \\ x_{i2} \\ \vdots \\ x_{ip} \end{pmatrix} \quad \xrightarrow{\hspace{1cm}} \quad \mathbf{X} = \begin{pmatrix} x_1^T \\ x_2^T \\ \vdots \\ x_n^T \end{pmatrix}$$

- Dataset $\{(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)\}$

- Course bureaucracy
 - Material and Schedule
 - Exam and grading
- Course topics
 - Statistical learning
 - Regression
 - Classification
 - Clustering
- Notation
 - Input/Output, Feature/Class, Data/Clusters, ...
 - Consistent matrix notation



- Next week lecture will be about the R language
 - Bring your laptop to practice yourself (suggested)
 - Install already  R Studio
 - By installing it you get the right 
 - You can follow the links from here

<http://davide.eynard.it/pami-20152016-lab-01/>